

Sensitivity Analysis of Pile Supported Wharves against Directional Uncertainty of Earthquakes Using Fragility Curves

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ABSTRACT

This paper aims to tackle an important uncertainty which extremely affects seismic performance of wharf structures in earthquake events. According to previous studies performed for structures on land, it is shown that structures on land are highly susceptible to unknown orientation of earthquakes called as the directional uncertainty. However, for marine structures, especially pile supported wharves, research efforts are rare to assess the effect of directional uncertainty of earthquakes on structural responses. Therefore, to show this effect on seismic performance of pile supported wharves, fragility analysis is performed based on methodology suggested by Pacific Earthquake Engineering Research Center (PEER) for the modeled pile supported wharf located in Maah-shahr port as a case study. As the first phase of this methodology, nonlinear static pushover analyses are performed for randomly chosen incident angles in order to quantitatively measure damage states suggested by marine design code. After damage states are obtained, IDA analyses are conducted in the selected incident angles to obtain nonlinear structural responses which are supposed to be used for fragility analysis as inputs. Finally, once fragility curves have been developed according to the last phase of PEER methodology, the more vulnerable direction(s) of wharf from those incident angles is represented.

1. Introduction

Traditional seismic design philosophy has constantly been revised due to sever damages that structures have experienced in high intensity earthquakes [1]. Recently, structures have been designed to prevent buildings from low-intensity damages and total collapse. However, it was perceived that there were other important factors like the economic loss due to downtime and repair cost after the 1994 Northridge and 1955 Kobe earthquakes [2-4]. Therefore, early forms of performance-based earthquake engineering (PBEE) which explicitly considered post-earthquake condition of structures were proposed (ATC-32, ATC-40, FEMA 273, SEAOC vision 2000, and so on). One of the primarily restriction of this version was that the major portion of it was based on simplified techniques (such as prediction and definition of seismic hazard, methods of structural analysis, prediction of component, and structure performance) and did not consider new scientific advancement and information. Therefore, Pacific Earthquake Engineering Research Center (PEER) proposed a systematic methodology which seeks to thoroughly assess individual components related to earthquake engineering and to provide the

probabilistic framework which combines these components for the seismic design and assessment of structures in conjunction with the most recent development in engineering science. Since the procedure of this framework is carried out based on a probabilistic manner, it can take uncertainties into account [5-6].

Along with the recent developments in design philosophy, one of the developments in earthquake engineering in analytical approaches has been Incremental Dynamic Analysis (IDA) method proposed by Cornell et al in 2002, which is well integrated into this probabilistic framework. The basis of IDA is a parametric analysis method to accurately calculate nonlinear structural responses under seismic loads. The procedure of IDA involves subjecting a structural model to ground motion time series, each scaled to multiple levels of intensity, in main principle directions of structure, thus producing one (or more) curve(s) of response parameterized versus intensity level [7]. However, apart from well integration of IDA into the framework, there are some uncertainties that affect the outcome of IDA [8]. Some of these uncertainties are structural, geotechnical, and seismic

parameters measured for structures in form of one report released by (PEER) in 2006 [9], and various studies were carried out to measure effect of these uncertainties on marine structures. In 2007, Na et al investigated the effect of geotechnical uncertainty on PC1 berth damaged in Kobe earthquake event. In this study. It was shown that friction angle and shear modulus of soil contributed most to variability of structural responses [10]. In 2009, Na et al investigated the effect of soil property uncertainties on the wharf located in western part of United states, and they developed fragility curves for the wharf with and without considering effect of uncertainty. Finally, in this study, it was shown that the results obtained without considering the geotechnical uncertainties were underestimated [11]. In 2013, Heydari-Torkamani et al measured the effect of uncertainty in geotechnical and structural parameters of a pile supported by performing sensitivity analysis based on IDA approach. In this study, it was shown that friction angle and porosity of rock fill as the geotechnical parameters and dead load of the structure as the structural parameter affected seismic responses of the analytical approach most [12]. In addition to geotechnical and structural uncertainties, there are some seismic uncertainties with a considerable effect on structural responses. Although IDA deals with existing uncertainty in set of ground motions well, there is another type of seismic uncertainty which noticeably affects seismic demand especially in the inelastic zone. This uncertainty stems from existing uncertainty in unknown orientation of earthquake called as directional uncertainty. There are different investigations evaluated directional uncertainty for structures on land, especially. In 2010, Lagaros investigated the effect of directional uncertainty on IDA approach and integrated this approach with directional uncertainty introduced as Multicomponent Incremental Dynamic Analysis (MIDA) method. In this method, two components of earthquake were applied to structures with variation of incident angles from 0 to 360 degree to show variation of structural responses against different incident angles [13]. In 2017, Rupali et al used response spectrum method to evaluate demand response in different incident angles, from 0 to 90 degrees with an increment of 10 degrees, and the variation of responses against different incident angles was concluded [14].

According to the previous studies, the importance of considering uncertainties in performing a structural analysis is undeniable since the outcome of structural analysis is supposed to be used as an input for risk assessment of a structure by using fragility analysis. Therefore, the more reliable and accurate responses are obtained by the structural analysis, the more reliable results are concluded by fragility analysis. Recently, fragility analysis has been used as an efficient tool for the risk assessment of wharf structures. In 2011, in a

dissertation, Shafieezadeh developed fragility curves for different components of one wharf, pile sections, pile-deck connection, relative movement of the wharf with respect to the land slide crane rail for two-dimensional and three-dimensional nonlinear models. The results of analysis revealed that the relative movement of the wharf with respect to the land slide crane rail was the most susceptible component in the earlier step of fragility analysis. In addition, pile sections showed extreme vulnerability in high intensities [15]. In 2011, Chiou et al modeled port of Taiwan and developed fragility curves by Capacity Spectrum Method (CSM) in order to assess seismic performance of the port [16]. In 2012, Thompolous et al developed fragility curves for a typical pile supported wharf in Los Angles through proposing a methodology based on a nonlinear dynamic analysis [17]. In 2012, Yang et al developed two sets of fragility curves by performing nonlinear time-history analyses for two wharves with cranes in Los Angeles and California [18]. In 2014, Heydari-Torkamani et al analyzed a pile supported wharf by IDA and assessed seismic vulnerability of pile-supported wharves by developing fragility curves [19]. In 2016, Banayan-Kermani et al considered the pile supported wharf located in harsh environment of Persian Gulf. In this study, they induced the aging effect to the model and evaluated the effect of FRP layers as a common retrofit method on the damaged model by developing fragility curves [20]. In 2016, Kermani et al conducted a survey on the importance of fragility curves in seismic vulnerability assessment of pile-supported wharf and indicated an importunate need to develop the application of fragility curves for marine structures [21].

The previous studies show the importance of uncertainties in performing structural analysis which is the main basis of probabilistic framework of PBEE, and disregarding these uncertainties weaken the reliability and accuracy of output of this framework, which is the result of fragility analysis. Since less efforts are made for measuring the effect of directional uncertainty on seismic performance of marine structures, this paper aims to assess influence of directional uncertainty over seismic performance of a prevailing pile supported wharf by developing fragility curves. For this purpose, the four-phase PBEE probabilistic methodology of PEER is considered to perform fragility analysis step-by-step. Initially, Port of Maah-shar is selected as an input for the methodology. Then, to evaluate directional uncertainty, various incident angles with a constant increment are randomly selected. As the first phase of methodology, a pool of eleven ground motions is selected, and structural analyses i.e. pushover analyses and IDAs are performed in the selected incident angles as the second phase. When the required inputs for the fourth phase are determined, fragility curves are developed for the

incident angles as the last phase of this framework. Finally, by comparing fragility curves, the more vulnerable direction(s) is concluded.

2- PEER PBEE analysis methodology

The PEER methodology with an iterative process includes 4 major steps as Figure 1: Hazard Analysis, Structural Analysis, Damage Analysis, and Loss Analysis. The results of each block are respectively represented as generalized variables: Intensity measure (IM), Engineering Demand Parameter (EDP), Damage measure (DM), and Decision Variable (DV). The iterative process of this methodology stems from finalizing an optimized input.

The relation between each block are mathematically represented by Total Probability Theorem Eq1.

$$P[DV|O,D] = \int \int \int p[DV|DM] p[DM|EDP] p[EDP|IM] p[IM|O,D] dIM dEDP dDM \quad (1)$$

Where O is Location of the structure, D is design of the structure, IM is intensity measure of earthquake site effects, EDP is engineering demand parameter as a measure of structural response, DM is measure of physical damage of various members, and DV is decision variable that is the performance parameter of interest such as report cost. The first step of this methodology is Hazard Analysis which produces one or more Intensity Measure (IMs). The IM which is typically represented by values of spectral acceleration or peak ground motion is used to show the strength or intensity of an earthquake. The second step is Structural Analysis. In this step, the desired structure is numerically modeled to predict EDPs in the given IMs. In fact, this step provides a link between IMs and EDPs by performing the structural analysis. The third step is Damage Analysis in which damage in structural and nonstructural analysis is predicted in accordance with EDPs, and damage measures (DMs), which are qualitatively defined by design codes, are physically identified in the numerical model. The relationship between DM and EDP is represented by

fragility curves, which gives the probability of being in or exceeding a DM given a value of EDP. The last step of this methodology is Loss Analysis. This analysis mainly discusses the meaningful value for an owner or decision maker of the structure. This value includes direct pecuniary losses, casualties, and downtime [5]. In the following, a case study is considered to develop fragility curves through the procedure of PEER methodology. It is worth mentioning that the last phase of PEER methodology which is Loss Analysis is excluded since the aim of this paper is to assess the effect of directional uncertainty on pile supported wharves by developing fragility curves.

2-Facility definition

As the first phase of methodology, one structure has to be selected and designed. Therefore, wharf No.1 of Maah-shahr port located in Iran is considered as a case study (Figure 2-a). This port is $20\text{ m} \times 45.6\text{ m}$ in plan ($4@5\text{ m}$ span in transverse direction and $8@5.7\text{ m}$ span in longitudinal direction). In addition, it has 32 prestressed concrete (PC) vertical piles and 4 PC batter piles of class c. The batter piles inclination is 41 degrees comparing to the coast line. To model this wharf, SAP2000 software is used, and the 3D view of model is shown in figure 2-c [22]. In this model, properties of soil layers are shown in Table 1. Soil-pile interactions are modeled by Winkler's plastic springs (P-Y and T-Z curves) suggested by API standard [23]. Since the place where plastic hinge occurs is not obvious, plastic hinges are distributed and modeled on piles as Figure 2-e. In this figure, ductile plastic hinges are allowed to form at the cap piles and seabed where piles interact with soil. The modal analysis of this model reveals that the fundamental periods of model are $T_x=1.68\text{ sec}$ and $T_y=1.63\text{ sec}$ in strong and weak axes (i.e. O_x direction and O_y direction), respectively.

3- Structural Analysis and Hazard Analysis

The next phases of this methodology are followed by conducting Structural Analysis and Hazard analysis which are usually performed simultaneously. The structural analysis is frequently started by nonlinear

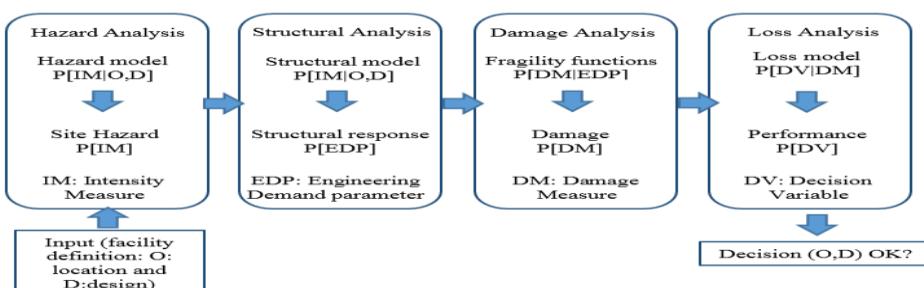


Figure 1. PEER (Pacific Earthquake Engineering Research center) PBEE analysis methodology [5]

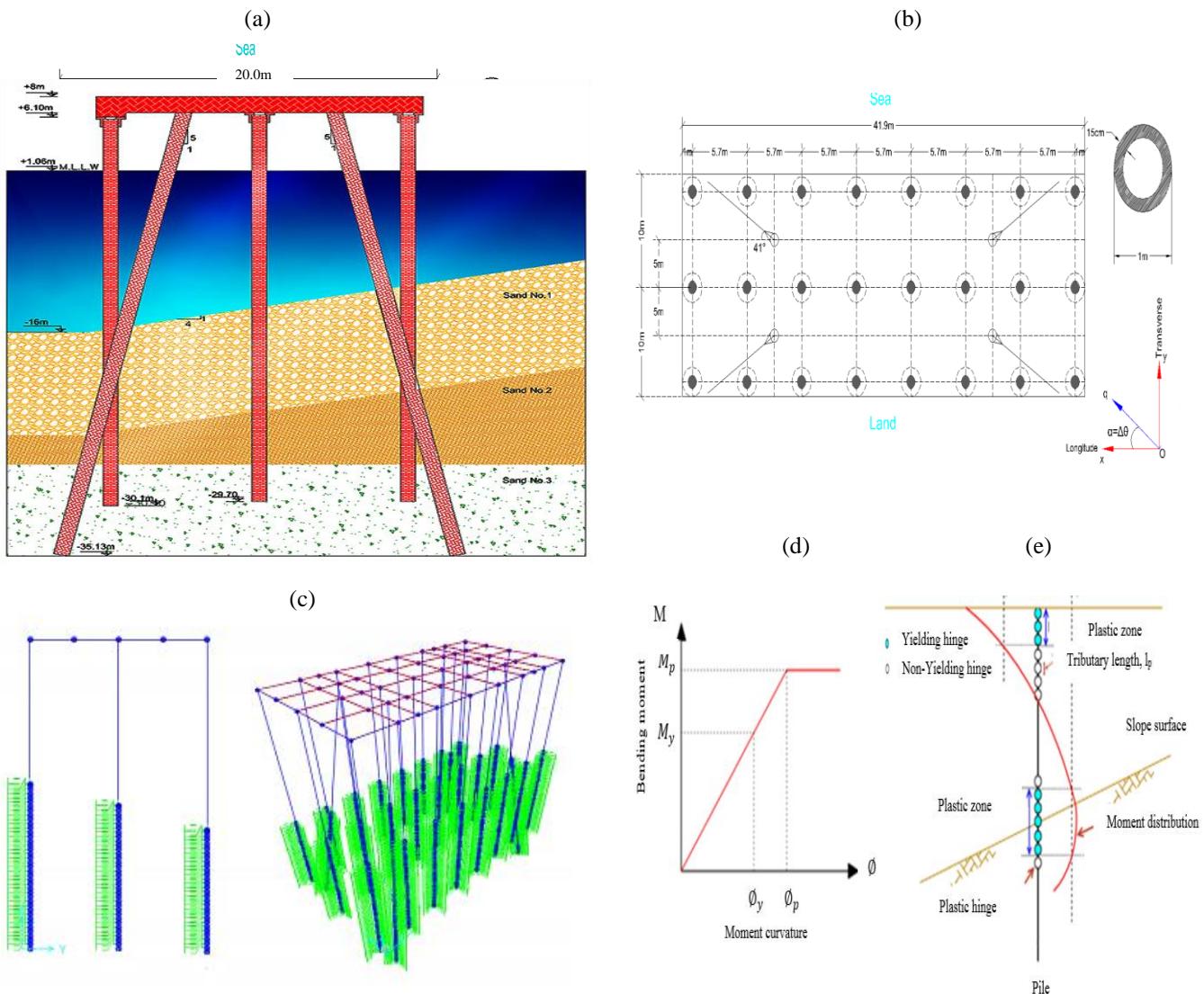


Figure 2. Maah-shahr wharf: (a) section (b) plan (c) Maah-shahr port in SAP2000 software. (d) moment-curvature curve of piles (e) distribution of plastic hinges on piles [19].

Table 1. Properties of soil layers in Maah-shahr port, wharf No.1.

No.	H(m)	$E(\frac{Kg}{cm^2})$	$\gamma_d(\frac{Kg}{cm^2})$	$C(\frac{Kg}{cm^3})$	$\Phi(deg)$
1	10.5	40-55	1.4-1.5	0.15-0.2	0
2	1.0	80-160	1.4-1.55	0.3-0.6	0
3	23<	350-450	1.55-1.75	1.5-2	0

pushover analysis in order to determine damage measures required for the damage analysis. According to PIANC, damage measures are qualitatively represented as table 3 [24].

To obtain the quantities of damage measures based on PIANC suggestion, pushover analyses are performed along all directions from 0 to 180 with an increment of 22.5 degrees. These damage measures are specified in accordance with the occurrence of plastic hinges which are defined along Ox and Oy during the analyses. The results are shown along Ox and Oy to trace the trend of global instability in the structure better (Figure 3).

Table 2. Different damage states suggested by PIANC for piles of wharf structures [24].

Damage states	Degree I: Serviceability	Degree II: Repairable	Degree III: Near Collapse
Pile (peak response)	Essentially elastic response with minor or no residual deformation	Controlled limited inelastic ductile response and residual deformation intending to keep the structure repairable	Ductile response near collapse (double plastic hinges may occur at one or limited number of piles)

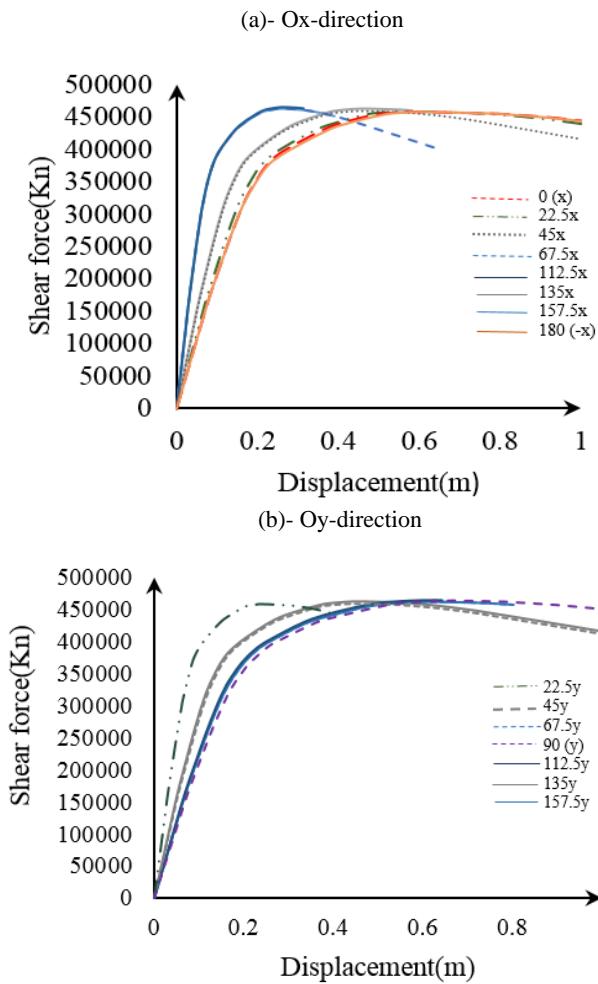


Figure 3. Pushover results of wharf No.1 in Maah-shahr port in (a) Ox-direction (b) Oy-direction.

After the pushover analyses, the structural analysis is continued by performing one dynamic analysis. According to previous studies, one of the common dynamic analysis which is well integrated to this frame work, especially when seismic uncertainty is under question, is IDA method [5]. There are two important steps in basis of IDA method. These are selecting a proper IM (Hazard Analysis) to scale selected ground motions and an appropriate EDP to develop IDA curves. There are different common IMs and EDPs for performing IDA method. The former is Peak Ground Acceleration (PGA), Peak Ground Velocity (PGV), and the $\xi=5\%$ damped spectral acceleration at the structure first at the structure first mode Sa (T1, 5%). The latter is maximum base shear, nodal rotation, peak story ductility, peak roof drift, and the maximum peak inter story drift angle (θ_{\max}) could be chosen [6]. For scaling selected ground motions, Amirabadi et al suggested that selecting Sa (T1, 5%) as IM in IDA approach [25], and for developing IDA curves, PIANC is recommended to record peak response of piles as EDP. Therefore, after 11 time histories are selected as table 4 and Figure 4 from PEER database [26], they are scaled by Sa (T1,5%). The major characteristic of scale factors is having structural responses changed from elastic to plastic zone. Then, IDA is performed for the

incident angles as the pushover analyses, and IDA curves are developed in the monitored directions of Ox and Oy by the selected EDP. It is a common practice to perform IDA for strong and weak axes. To show the effect of directional uncertainty on IDA responses, IDA is initially performed for 0, 90, 112.5, and 22.5 incident angles (Figure 5). Subsequently, they are summarized for different fractiles (16, 50, and 84%) at each level of intensity (Figure 6). For the other incident angles, the same step is taken, and the summarized capacities obtained by IDA are displayed in Figure 8. According to this figure, the bearing capacity of structure depends on Oy direction for the incident angles around 90 degrees and on Ox direction for the incident angles around 0 and 180 degrees.

Table 3. The damage states for each direction (cm)

Damage measures	Serviceability (I)		Repairable (II)		Near Collapse (III)		
	Monitored directions	Ox	Oy	Ox	Oy	Ox	Oy
Incident angle	0	14.95	-	45.73	-	76.51	-
	22.5	14	6	42.5	18	71	30
	45	10	10	31.5	31.5	53	53
	67.5	5	14	16.5	41	28	68
	90	-	16.72	-	43.36	-	70
	112.5	6	14	16.5	39.25	27	64.5
	135	10	10	32	31.77	54	53.5
	157.5	6	14.4	17	41.5	29	69
	180	16	-	46.85	-	78	-

Table 4. The ground motion records selected from PEER database [26].

Event	Station	M	R(Km)	PGA(g)
Northridge	Lake Hughes	6.69	35.81	0.08
Cape Mendocino	Fortuna	7.01	16.54	0.116
Loma perieta	Anderson dam	7.1	24.32	0.247
Morganhill	San justo dam	6.19	45.47	0.079
Sanfernando	Pearblossom Pump	6.61	35.54	0.091
landers	Desert Hot Spring	7.28	21.78	0.139
San fernando	Pasadena	6.5	40	0.098
Manjil	Abbar	7.37	12.55	0.359
Loma perieta	Fermon	7.1	39.04	0.127
Loma perieta	Montary	7.1	54.86	0.073

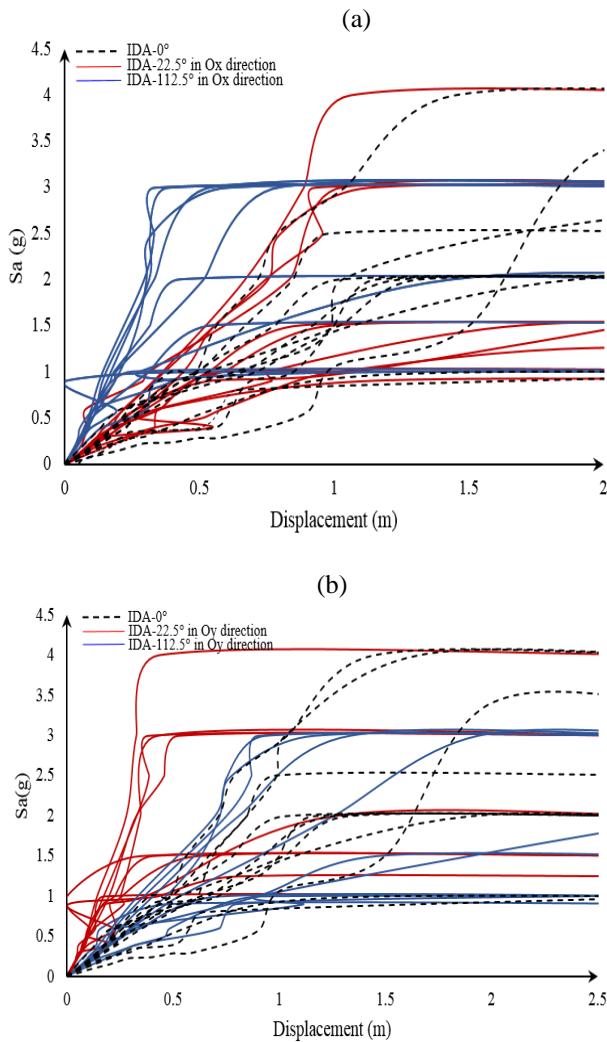


Figure 5. multi-recorded IDA (a) in 0, 22.5, and 112.5 degrees along Ox direction (b) in 0, 22.5, and 112.5 degrees along Oy direction.

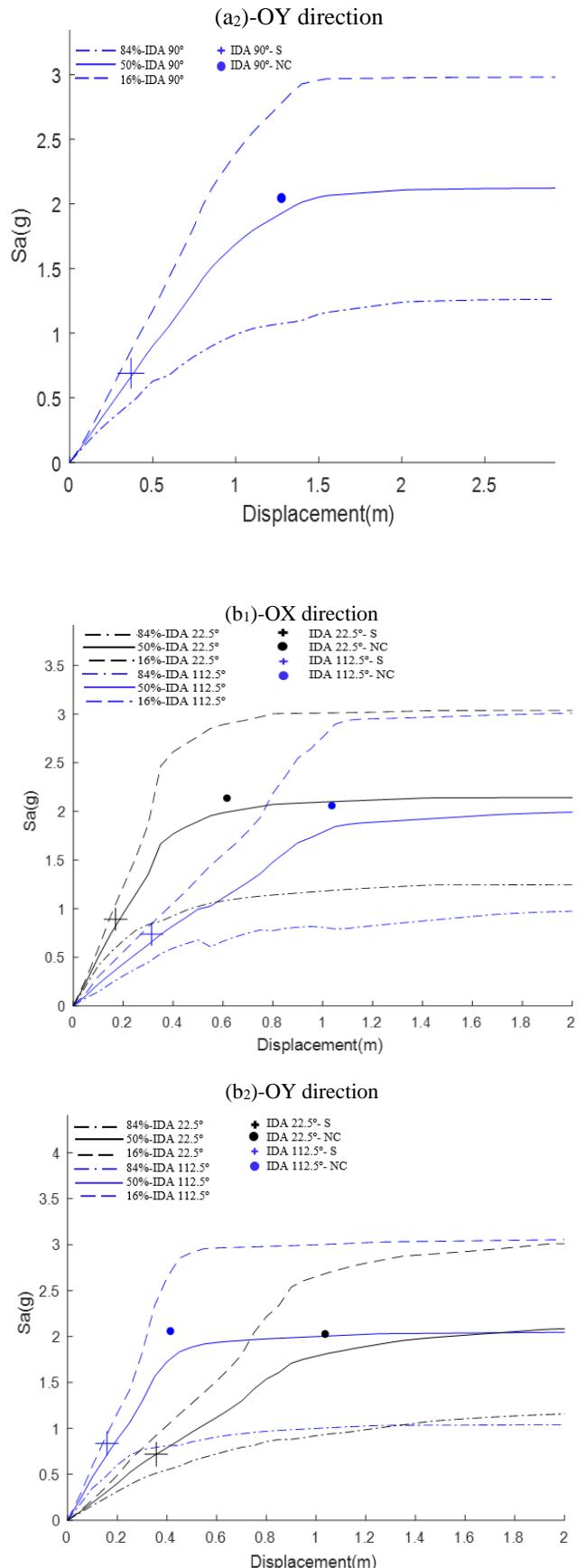


Figure 6. 16, 50, and 84 % fractiles of IDA curves in Ox and Oy directions: (a1) 0 degree (a2) 90 degrees, (b1) 22.5 degrees, (b2) 112.5 degrees.

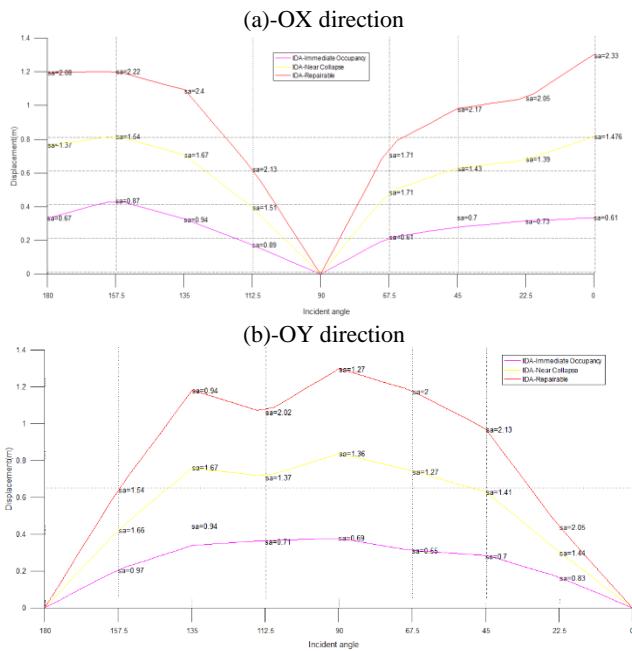


Figure 8. Summarized capacities of IDA in Ox and Oy directions for each incident angle.

4-Damage Analysis (Fragility Analysis)

To perform damage analysis, the outputs of previous phases i.e. EDPs and DMs are used for the fourth phase. In this phase, the conditional probability of wharf responses exceeding damage states of s_i at a specific PGA level is obtained as fragility curves (Eq.2) [16].

$$P[S > s_i | PGA] = P[X > x_i | PGA] = 1 - \Phi \left[\frac{\ln x_i - \lambda}{\zeta} \right] \quad (2)$$

Where Φ is normal cumulative distribution function, x_i is the upper bound for s_i (i=I,II,III), and λ and ζ are mean value (μ) and standard deviation (σ) of sample population (x) in each scaled level (Eq.3, 4, and 5).

$$\lambda = \ln \mu \frac{1}{2} \zeta^2, \quad \zeta^2 = \ln [1 + \delta^2], \quad \sigma = \frac{\sigma}{\mu} \quad (3,4,5)$$

As a common post processing of developed fragility curves, it is typical to use simplified fragility curves. These curves are typically expressed by lognormal distribution functions (lognormal CFD). Using lognormal CFD makes the application of fragility curves more convenient (Eq.6).

$$F_A(a) = \int_0^a \frac{1}{\sqrt{2\pi}\zeta A} \exp \left[-\frac{1}{2} \left(\frac{\ln a - \ln m_A}{\zeta A} \right)^2 \right] da \quad (6)$$

Where A is the random variable of the PGA, m_A is the median of A, and ζA is the logarithmic standard deviation of A. In figure 9, fragility curves are developed for each incident angle and shown for different damage states. According to this figure, the seismic performance of wharf is affected by directional uncertainty as the intensity of earthquakes increases, and in some incident angles plastic hinges occurred sooner than the others. For the serviceability damage state among these incident angles, the critical direction is 157.5 degrees where the probability of exceeding the

damage state in a lower Sa is higher than the others in Oy direction. For the repairable damage state among these incident angles, the critical direction is 45 degrees where the probability of exceeding the damage state in a lower level of intensity is higher than the others in Ox direction. For the near collapse damage state, the critical direction among them is 0 degree which reaches to global instability in a lower level of intensity comparing to the others.

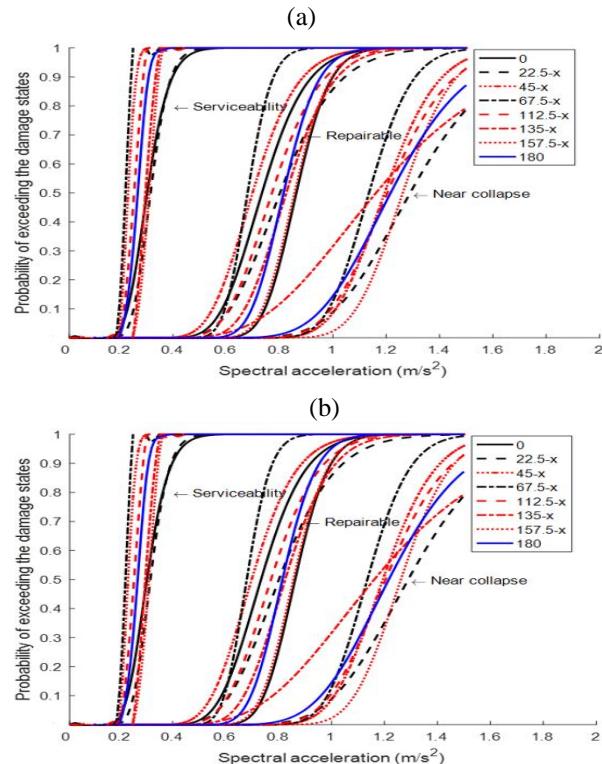


Figure 9. fragility curves in each incident angle for all damage states (a) Ox direction (b) Oy direction.

5-CONCLUSION

In this paper, the systematic methodology of PEER PBEE analysis is adopted in order to assess seismic performance of the pile supported wharf of Maah-shar against directional uncertainty of earthquakes. According to step-by-step procedure of the four-phase methodology of PEER, 11 ground motions are selected, and pushover analyses and IDAs are performed to measure DMs and EDPs, respectively. To show the effect of directional uncertainty on seismic performance of the wharf, the third phase of this methodology is performed by developing fragility curves. By comparing fragility curves, it is shown that the severity of directional uncertainty reveals when the damage measures change from moderate damage to extensive damage. In addition, by using and comparing fragility curves for the selected incident angles, the critical directions among these incident angles for serviceability, repairable, near collapse damage states are 157.5 degrees in Oy direction, 45 degrees in Ox direction, and 0 degree with a high probability of occurrence, respectively.

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